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# Auroral ionospheric conductivities: a comparison between experiment and modeling, and theoretical $f_{10.7}$ -dependent model for EISCAT and ESR

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**Abstract.** Several authors have published models of auroral conductances in the past. Some of them are based on theoretical approaches; others are the result of observations. The data bases for the latter models range from 8 h to 3 years of experiments. In this paper, we show the results of our own modeling, based on a coupled kinetic/fluid approach. We compare these results to the statistical model based on 3 years of experiment. We then model the auroral ionospheric conductances above EISCAT and the EISCAT-Svalbard Radar for different solar-activity indices. These modeled conductances are fitted with a simple law depending on the  $f_{10.7}$  index and on the solar zenith angle.

## 1 Introduction

Hall and Pedersen conductivities are essential parameters for the description of ionospheric phenomena and magnetosphere coupling. Therefore, many authors have tried to model them, or deduce them from incoherent-scatter radar measurements. A very good review of most of the models can be found in Brekke and Hall (1988); the authors also discuss the proper choice of parameters, such as the collision frequency models, and that will therefore not be discussed again here; nor will the other models be presented. The important thing about those models is that they are based on sparse data bases, ranging between a few hours to 27 days of data. Most of the radar data for those models come from Chatanika or EISCAT experiments. The geophysical conditions vary from  $f_{10.7} = 81$  to 156. The main result is that conductivities may take any value in a margin too large to be informative (for example, the Pedersen conductivity ranges between 5 and 12 MHOS at a solar zenith angle of  $0^\circ$ , depending on the model used).

Since that time, a step forward has been taken with the statistical study of solar contribution to auroral height-integrated conductivities (Senior, 1991). The author processes 3 years of EISCAT data in order to deduce a statistical model of conductances above EISCAT. The data are chosen from quiet conditions. This model is an improvement in the sense that it is based on a large data base, and so any theoretical computation should first be compared with this one. This is the aim of the first part of this paper, where we will discuss the assumptions made by Senior. This demonstrates the difficulties of the experimental approach, and shows the need for a theoretical model. We then propose a theoretical model for EISCAT diurnal conductances, depending on the solar activity. “Diurnal” is taken in the sense “only due to photoionization”. Finally, we also predict the diurnal conductances above the EISCAT-Svalbard Radar (ESR) for different solar activities. Another review paper that includes Senior’s model may be found in Brekke and Moen (1993).

We do not describe the two radars (EISCAT and ESR), since this is very well done in several papers. One can find most of the useful explanations on the diverse modes of the EISCAT radar in Rishbeth and Van Eycken (1993). The scientific objectives and the location of ESR, soon fully operational, are described in Bjorna *et al.* (1991).

## 2 Experimental/theoretical comparison

### 2.1 Description of Senior’s work

In order to perform a meaningful comparison, one needs to remember how the conductivities have been processed by Senior. From the EISCAT data base, she selected 3 years of CP-3 experiments for quiet conditions. At low altitudes, where only power-profile measurements are available, the author corrected the power-profile density assuming  $T_e = T_i = T_n$ . Since her purpose was to come up with a simple and very general formula for the integrated conductivities, she had to use very general parameters. For example, the magnetic field is kept constant (equal to

the value given by IGRF at 120 km). Since there is an asymmetry between the conductivities around noon due to the neutral atmosphere, the author chose a neutral atmosphere model which does not depend on the time. Then, the computation only depends on the solar zenith angle, and morning and evening data could be mixed (although the asymmetry also shows up in the electron density). This model is *vin2mil* (Alcayd , 1981). It proposes an analytical formula for the neutral temperature and densities which depends on a set of seven parameters, amongst which is the exospheric temperature. All of the seven parameters used in Senior's work are those published in the original paper of Alcayd  (1981), including the exospheric temperature set to 1000 K. The ion mass normally depends on the ion composition; but, in order to be again as general as possible, it was set to 30 amu. The formula for the ion/neutral collision frequency came from Brekke and Rino (1978), and has the advantage of being independent of the ion temperature. The electron/neutral collision frequency came from Banks and Kockarts (1973), and only depends on the neutral temperature and densities. With a careful analysis of the whole data base, Senior came up with 27127 blocks of data (each block corresponding to an electron density, and electron/ion temperature profile measurements), from 23 CP-3 experiments gathering about 900 h of data from June 1984 to November 1987. Those points are shown in Fig. 1. The mean *Kp* is 3. Then, the author extracted all data that could be perturbed by precipitation. This selection procedure is fairly complicated, and strongly depends on the criterion used. In Senior's article, the selection has been made using a statistical model by Hardy *et al.* (1987). Once this is

done, about 9000 profiles were left for the computation of the integrated conductivities. The resulting seasonal distribution of the data base had no point during winter (21 December to 21 March). The computation of the conductivities was carried out using the usual formulas:

$$\sigma_p = \frac{N_e e}{B} \left[ \frac{\omega_e v_{en}}{\omega_e^2 + v_{en}^2} + \frac{\omega_i v_{in}}{\omega_i^2 + v_{in}^2} \right], \quad (1)$$

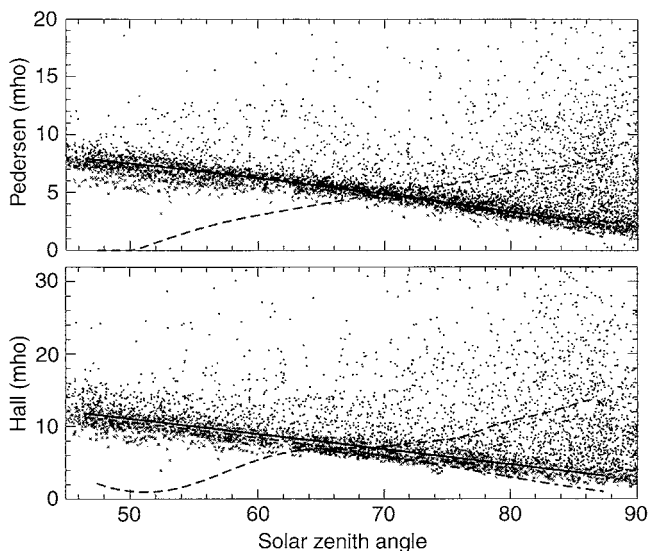
$$\sigma_H = \frac{N_e e}{B} \left[ \frac{\omega_e^2}{\omega_e^2 + v_{en}^2} - \frac{\omega_i^2}{\omega_i^2 + v_{in}^2} \right], \quad (2)$$

where  $\sigma_p$  and  $\sigma_H$  are, respectively, the Pedersen and Hall height-dependent conductivities,  $N_e$  represents the electron density,  $\omega_{e,i}$  the electron/ion gyrofrequencies,  $v$  is the collision frequency, and  $B$  the magnetic field strength. Senior then fitted a height-integrated conductivity model to the data base. This model, referred to hereafter as CS, is also shown in Fig. 1, and constitutes the basis for our comparison. It predicts the conductances due only to the photoionization.

## 2.2 Description of the modeling

TRANSCAR is a coupled kinetic/fluid transport equation code. It has been described in Diloy *et al.* (1996). The kinetic part consists in solving a stationary electron transport equation along the magnetic field line, taking into account the collisions between a hot population of electrons (photoelectrons and/or precipitation) and the neutral atmosphere. Collisions may be elastic and/or inelastic, leading to the computation of the ion production. The electron thermal gas heating rate through friction force is also computed. These parameters (ion production and electron heating rate) are then used as inputs to the fluid code. This part solves the eight moments of the time-dependent fluid equation, namely the densities (electron, ions: first moment), temperatures (electron, ions: second moment), velocity vector (three more moments), and heat-flux vector (moments 6 to 8). It should be noted that the electron density and temperature are inputs to the kinetic part, so that the coupling is dynamic. On our IBM RISC 590, eight CPU hours are necessary to describe 24 h of experiment (taking into account three simulated hours of blank run to make sure that the model is in an equilibrium state at the beginning of the modeled day), making it impossible to simulate all the 54 days of experiment, and then average the computed conductivities. One could gather the experimental days within a few blocks, each weighting the relative number of blocks of experiments. However, the problem of relative weight is not a simple one, since small zenith angles are only seen during summer. We therefore decided to run the code for only 1 day supposed to be statistically representative of the whole data base in terms of activity indices: Senior's data base had an averaged  $f_{10.7}$  of about 80, and a mean *Kp* index of 3, corresponding to an *Ap* index of 14. Then we shall study separately the effects of the change of neutral atmosphere through the season.

In order to cover the smallest solar zenith angles seen at EISCAT, we ran TRANSCAR on 21 June (day 183).



**Fig. 1.** CP-3-experiment data base used for the statistical study of Senior (1991). The points are those data excluded because they are thought to be due to precipitation. The *light crosses* are the data used for Senior's modeling. Although it is difficult to see, some points show up in the crosses at any angle, especially on the Pedersen conductance. The *full line* is the statistical model from Senior. The *dot/dashed line* is the modeling from TRANSCAR. Finally, the *dashed line* represents Hardy's statistical model for conductances due to precipitation

The atmosphere was given by MSIS 90 (Hedin, 1991), the magnetic field came from IGRF, the solar flux was inferred from those published and modified by Torr and Torr (1985) into 37 energy bins from 248 to 12.02 eV (17 discrete solar EUV lines and 20 energy intervals, with averaged fluxes). Following Tobiska (1993), two values were added at 2.327 and 3.750 nm to take account of ionization due to highly energetic photons. The  $f_{10.7}$  value and the  $A_p$  index used in our simulation were 80 and 14, respectively. These runs gave an estimate of the electron density. Then, using the same parameters and assumptions as Senior (including the upper altitude of integration), we computed the integrated conductivities. The result is shown in Fig. 1. The agreement between our modeling and CS was very good from  $45^\circ$  to  $78^\circ$  for the Pedersen conductance, with a discrepancy of less than 2%. For the Hall conductance, the agreement was correct from  $45^\circ$  to  $65^\circ$  at a precision of 3%, but the discrepancy increased as the solar zenith angle increased: at  $87^\circ$  the CS predicted value is 1.2 MHO higher than our modeling.

The fact that Pedersen conductance was in better agreement than the Hall conductance indicates that the differences between the computed electron density and CS-data-base electron densities mostly occurred below 115 km, since the Pedersen conductivity peaked near 120 km and was larger than the Hall conductivity above that altitude.

### 2.3 Discussion of the discrepancy

#### 2.3.1 Effect of the computer code

The discrepancy could of course be due to our computational model. The kinetic part has been widely tested against experiments and other models (Lummerzheim and Liliensten, 1994). One of the tests compared to the experiment in the following manner: Barrett and Hays (1976) shot different beams of electrons at collimated energies through a box filled with  $N_2$ . A photometer analyzed the intensity of the 391.4-nm emission line all along the box. We could reproduce this emission with the kinetic code with an accuracy of less than 5%.

The fluid part of the code has also been widely tested, from the point of view of the numerical approach (Robineau *et al.*, 1995) as well as against incoherent-scatter radar experiments (Robineau *et al.*, 1996) at altitudes where the kinetic part does not play any role. It was shown that this eight-moment approximation is adequate, if one excludes the  $H^+$  light ion at very high altitudes (above 2000 km) for which the approximation starts to fail when this ion reaches a supersonic regime.

The coupling of the two parts has been used to reproduce a 24-h EISCAT experiment conducted in March 1994. We could retrieve all the features of the experiment, not only on the electron density but also on the temperatures and velocity. This is shown in Blelly *et al.* (1996). Therefore, although one can never claim that a code is free of any error, we would look for other explanations regarding this discrepancy.

#### 2.3.2 Grazing incidence

Since the discrepancy occurs for solar angles  $65^\circ$  to grazing incidence, it is natural to question the validity of the Chapman function. We use an approximation by Smith and Smith (1972) that has the advantage of consuming very little CPU time. However, we compared the production computed with this approximation to the approximation due to Green *et al.* (1964) and to a full integration of the Chapman function along the line of sight to the Sun. The differences cannot explain a difference of 1 MHO on the conductivities.

#### 2.3.3 Geophysical explanations

By “geophysical”, we mean the effect of the bad choice of the day, or the bad choice of the activity indices. Such effects will be shown in the following section, on a computation that does not take CS parameters into account (but rather MSIS and other commonly used models). We explore these effects in the next section, but they cannot explain the discrepancy in question.

#### 2.3.4 EISCAT data analysis

Here, we want to evaluate the error due to the corrected raw-data. The power profile provides a raw density  $N$ ; the true electron density is deduced from:

$$N_e = \frac{1}{2} N_e^{raw} \left( 1 + \alpha_D^2 + \frac{T_e}{T_i} \right) (1 + \alpha_D^2) = \Psi N_e^{raw}, \quad (3)$$

where  $\alpha_D^2$  is a correction for the Debye length effect equal to  $7.3 \times 10^6 (T_e/N_e)$ , and the other parameters have their usual meanings (temperature, density). Setting  $T_e = T_i = T_n$  gives an electron density of

$$N_e^* = \frac{1}{2} N_e^{raw} (2 + \alpha_D^{*2}) (1 + \alpha_D^2) = \Psi^* N_e^{raw}, \quad (4)$$

with  $\alpha_D^{*2} = 7.3 \times 10^6 (T_n/N_e)$ . The relative error is  $\Delta = (N_e - N_e^*)/N_e = (\Psi - \Psi^*)/\Psi$ . Since the temperatures in CS work were measured above 120 km, one only has to compute the error below this altitude. In order to do so, we have run the theoretical model TRANSCAR for our reference quiet day ( $Kp = 3$ ,  $f_{10.7} = 80$ ) at the EISCAT latitude. One excludes any case with strong Joule heating, so that at low altitudes  $T_e$  is close to  $T_i$ .  $\Psi$  is computed using the temperatures from TRANSCAR, while  $\Psi^*$  is computed using the neutral temperature from vin2mil. We then compute  $\Delta$ , the relative effect of the correction. The error proves to be negligible above 95 km (less than 1%). It increases when one goes down to reach 4.5% at 90 km, i.e., a slight overestimation of the electron density and therefore of the integrated conductivities. But at these low altitudes, the electron density is small, so that the global overestimation of the integrated conductivities cannot be larger than 1%.

#### 2.3.5 Selection of the data for CS model

This selection is based on the statistical model of Hardy *et al.* (1985, 1987). These authors analyzed 14.1 million spectra from the SSJ/3 detector of the DMSP F2 and F4 satellite. They came up with an electron precipitation model and, using the functional relationship of Spiro *et al.* (1982) corrected by Robinson *et al.* (1987), could propose

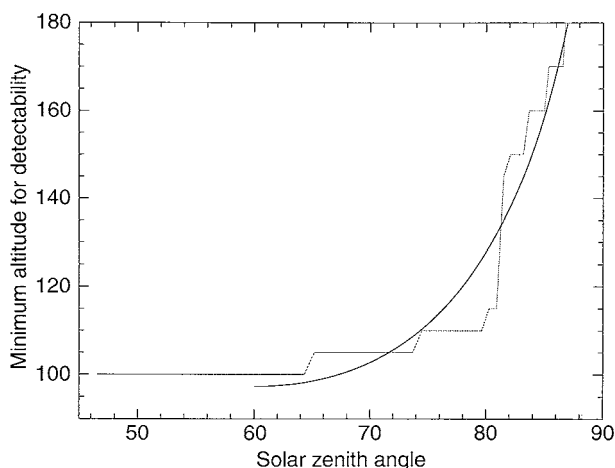
a statistical model of auroral conductivities due to particle precipitation which only depends on the geomagnetic coordinates and the  $Kp$  index. In order to go from an average integral number flux and an average integral energy flux of the precipitating electrons to the height-integrated Pedersen and Hall conductivities, the formulas used do not go through the computation of the electron density profiles. Senior (1991) stated that this process may well lead to an underestimation of the conductances in the evening sector.

Senior rejected an EISCAT density data set if, at its location, the modeled particle-produced conductance was larger than 1.5 and 2.1 MHO for the Pedersen and Hall conductances, respectively.

In Fig. 1 we also plotted the Hardy prediction for the conductivity due to particle precipitation above EISCAT on that same day (day 183, supposed to be statistically representative of the whole data base). It is very interesting to find out that the Hardy values cross the CS values at the solar angle where our computation starts to depart from CS model. Following Hardy's model, the conductances measured by EISCAT at high solar angle could, statistically, be due to particle precipitations.

### 2.3.6 EISCAT sensitivity

In the E region, EISCAT can detect electron densities above typically a few  $10^{10} \text{ m}^{-3}$ . We therefore checked at what altitude the TRANSCAR-computed electron density reaches the threshold of  $5 \cdot 10^{10} \text{ m}^{-3}$ . This is shown in Fig. 2. Below  $65^\circ$ , the electron density only reaches such low values in the very low E region, where the conductances are no longer important. At  $66^\circ$ , this threshold is above 100 km, and starts to affect the Hall conductance inferred from the EISCAT electron density measurement. It keeps going up to reach about 120 km at  $75^\circ$ . Then, the Pedersen conductivity also starts to be affected. The code covers the E region with 19 altitudes. The effect of the discretization is obvious in Fig. 2. We smoothed it with a simple polynomial which will be discussed in Sect. 4.



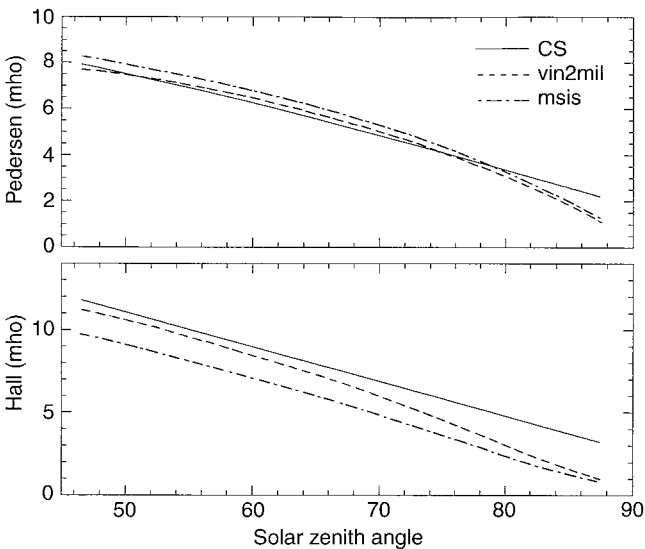
**Fig. 2.** The broken line shows the altitude above which the electron density is larger than the threshold of detection for EISCAT in the E region. The smoothed line follows the equation  $z = 361.8568 \cos \chi - 511.5282 \cos^{0.5} \chi + 278.1$  for solar angles  $\chi$  larger than  $60^\circ$

The conclusion of this section is that EISCAT has some difficulties in determining the conductances only due to solar photoionization typically above  $65^\circ$  solar angle from the power-profile measurement or for typical integration times of few minutes. What Senior (1991) has seen are conductivities due to particle precipitation, as confirmed by the statistical model of Hardy *et al.* (1985, 1987). At angles where the ion production due to photoionization is larger than the detectability threshold at all altitudes in the E region, our model fits the CS prediction very nicely. This may be confirmed by a comparison between CS (and the other models) and a DMSP/Sondrestrom coordinated experiment (Watermann *et al.*, 1993). In this paper, height-integrated electrical conductivities are deduced using radar and spacecraft measurements in combination with atmospheric and ionospheric models to distinguish between the contribution of the two main sources of ionization of the thermosphere during solar minimum. What is found is that for angles above  $60^\circ$ , the solar radiation components of the Pedersen and Hall conductances are systematically overestimated by the models in about the same proportion as that found in the present study. We therefore think that TRANSCAR proves to be a useful tool for modeling diurnal conductivities.

## 3 Influence of various parameters

In this next section, we replace all the specific parameters used by Senior (1991) for her statistical study by the usual parameters: the ion mass and the magnetic field intensity depend on the altitude, the neutral atmosphere is MSIS 90 (Hedin, 1991), the ion/collision frequencies depend on the ion temperature (see for example the review by Brekke and Moen, 1993), the integration upper limit is 600 instead of 200 km, the electron and ion temperatures are never set to the neutral one but computed by TRANSCAR. All these changes lead, of course, to a big change in the results, as shown in Fig. 3. In this figure, the conductivities are computed in the evening sector, the solar angle increasing from  $45^\circ$  to  $86^\circ$ , so that the comparison makes sense. It results in an increase in the Pedersen conductivity of about 0.6 to 0.7 MHO at low angle and 0.2 MHO at  $87^\circ$ , and a decrease in the Hall conductivity reaching 1.3 MHO at low angle. This is mostly an effect of the neutral atmosphere model. The differences between vin2mil and MSIS will not be discussed here, this being beyond the scope of this paper.

We now keep the last computation (based on “usual” parameters) to compare it with computations under different changes. As shown by Brekke and Hall (1988), Schlegel (1988), and Beaujardiére *et al.* (1991), electron densities above 200 km are expected to contribute at most a few percent to the daytime Pedersen conductance and nothing to the Hall one. In Fig. 4 we averaged the height conductance profiles over the whole set of computation; panel B shows the percentage of integrated conductivity versus altitude. One sees that integrating only to 200 km leads to the loss of about 7% of the Pedersen conductance and, as expected, nothing to the Hall conductance. In order to get a good estimate of the Pedersen integrated conductivity, one should integrate up to 300 km.

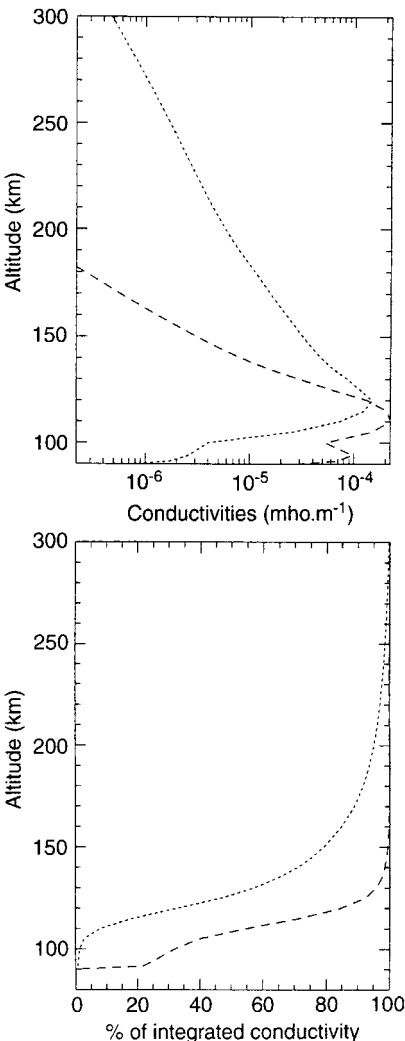


**Fig. 3.** Hall and Pedersen integrated conductivities. The *dashed* line represents the results of TRANSCAR computation with Senior’s parameters. The *dot-dashed* line is the same computation with usual parameters (see text). The *full* line shows CS model

Brekke and Hall (1988) have already studied the influence of the set of collision frequencies. That will therefore not be repeated here since our study agrees fairly well with their conclusions. They note that for the collision frequency model given by version 1 used in CS, the Pedersen profile has its maximum at greater heights than for the model given by version 2 (with  $T_e$ -dependent collision frequencies), and that the Hall conductivity profile is enhanced at greater heights for model 1 than for model 2. Their study and comparison with experiment use model 2.

Table 1 shows the influence of the variation of several parameters in the computation of the conductances. The magnetic field directly influences the conductivities, as well as indirectly through the gyrofrequencies. Its variation then has an important effect on the conductivities: increasing it by 5% leads to a decrease of about 10% in the Hall and 8.7% in the Pedersen conductance. An ion composition made up of 100%  $O_2^+$  or  $NO^+$  ions has little influence on the Hall conductance, but strongly increases the Pedersen conductance. In the test run, the composition is as follows: we compute the  $O^+$  composition (which is of course unimportant at such low altitudes) from the time dependent model from Chantal Lathuillère (Blelly *et al.*, 1996), and then make the assumption that the molecular ions are made up of 50%  $O_2^+$  and 50%  $NO^+$ . Changing this ratio has little influence on the global ion mass but changes the ion/neutral collision frequencies. The multiplication of the collision frequencies by a factor of 2 increases the Hall conductance by about 38% and the Pedersen conductance by about 30%. Since the  $O^+$  ion is not abundant at altitudes where the conductivities are large, the Burnside factor has almost no influence.

In Fig. 5 we plotted the reference computation (based on “usual” parameters and for day 183) versus the computation for day 80, in order to check the influence of the period of the year on the conductivities at a given solar

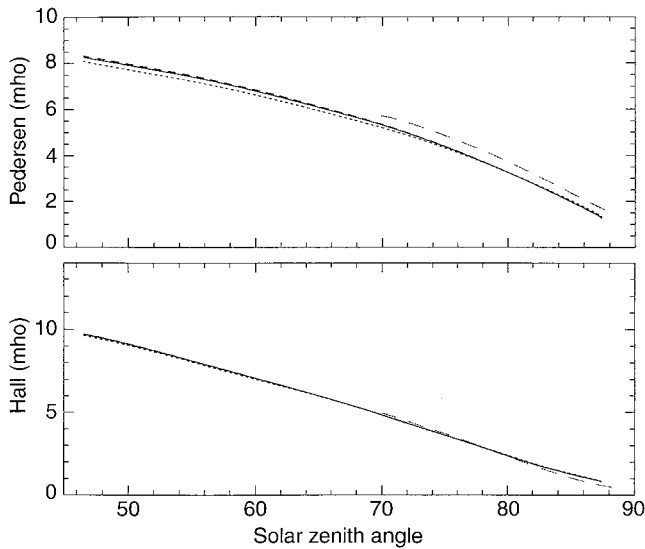


**Fig. 4.** The panel on the *top* shows the height profile of the Hall (*dashed* line) and Pedersen (*dotted* line) conductances, obtained by averaging a 12-h run of our model. The *bottom* panel shows the percentage of explanation of the conductances versus altitude

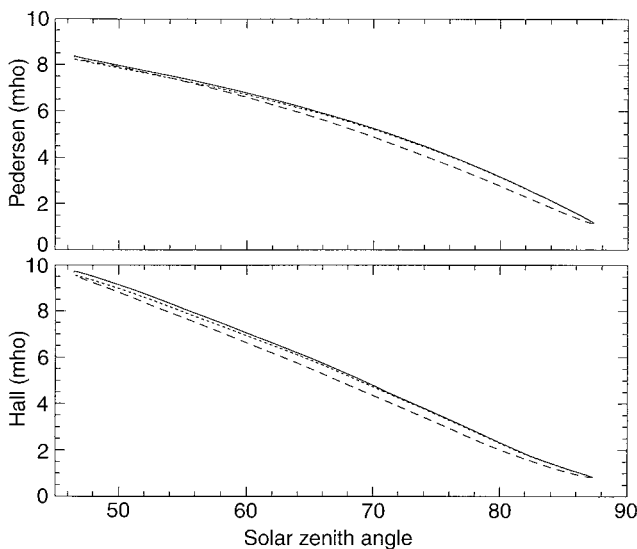
**Table 1.** Numerical influence of several parameters on a given “representative” run

	Hall conductance	Pedersen conductance
Test run	6.448	5.876
1.05B	5.801	5.36
100% O	6.664	7.196
100% NO <sup>+</sup>	6.606	7.052
2v <sub>in</sub>	8.894	7.638
Burnside = 1	6.440	5.763

zenith angle. On day 80, the solar angle only rises to 70°; the effect on the Hall conductance is negligible, but the Pedersen conductance increases by about 0.5 MHO due to the change in the neutral atmosphere. In the same plot we show the effect of the  $Ap$  index; for the test run it is set to 14. We show the conductances for  $Ap = 3$  and 20, which are typical margin values for  $f_{10.7} = 80$ . The effect of this change on both conductances is negligible.



**Fig. 5.** The full line is the TRANSCAR computation with usual parameters. The thin-dashed line is the same computation with  $A_p = 20$ . The dotted line represents the computation for  $A_p = 3$ . Finally, the large-dashed line is the computation for day 80



**Fig. 6.** Morning (dashed lines)/evening (full and dotted lines) conductances; see text for further details

Figure 6 shows the conductances computed with “usual” parameters for a 36-h run starting at 12 UT on 21 June and ending at 24 UT on 22 June. The neutral atmosphere given by MSIS is not the same in the morning and evening, so that the conductivities may be different at a given solar zenith angle in the evening and in the morning sectors. We therefore kept apart the conductivities from the two afternoons and from the morning of 22 June. This figure reads starting at 12 UT on 21 June on the top left corner of each panel; it follows the full line to go to sunset on the lower right part of each panel. Then the sun rises again on 22 June and the conductivities follow the dashed lines towards the left. An angle of  $70^\circ$  is obtained at 18.3 LT on the full line and at 5.7 LT on the dashed line.

Finally, one passes midday at noon on 22 June and goes to midnight: the conductances are then represented by the dotted lines.

At equal solar zenith angle, the evening (from noon to midnight, full and dotted lines) Pedersen conductance is up to 0.4 MHO larger than in the morning (from midnight to noon, dashed line), which represents a relative variation of about 10% at a solar zenith angle of  $70^\circ$  on the Pedersen conductance. The effect on the Hall conductance is not as large as on Pedersen (about 5% maximum), but lasts for a larger range of solar angles (from  $50^\circ$  to  $80^\circ$ ). This morning/evening effect has been already found experimentally by Senior (1980), using data from the French incoherent-scatter radar in Saint Santin. The modeled and experimental morning/evening asymmetries agree very well. From one day to the next, there is a small difference at noon of about 0.1 MHO on the Pedersen and 0.2 MHO on the Hall conductance. This difference vanishes as one approaches large angles. This is mainly an effect of the neutral atmosphere: on day 183, one reaches large angles. This is mainly an effect of the neutral atmosphere: on day 183, one reaches the solar zenith angle of  $46.58^\circ$ , while the minimum angle is  $46.66^\circ$  the next day. Even such a small difference produces relative differences of about 0.1% on the neutral temperatures and densities given by MSIS90. This difference is maximum for  $O_2$  and for the temperature at 110 km, affecting the Hall more than the Pedersen conductivity. The effect is enhanced by the fact that the neutral atmosphere enters the computation of the conductivities through the collision frequencies in the denominator only for the Hall conductance, but on both denominator and numerator for the Pedersen conductance (Eqs. 1 and 2).

#### 4 EISCAT and ESR conductances

We ran our code for different solar activity levels at EISCAT and ESR latitudes. We show here the result of this modeling of the evening conductances, in order to propose a simple model depending only on the solar zenith angle. In order to use to compare with instantaneous measurements, one should use the study of the preceding section to proceed to corrections.

We varied the  $f_{10.7}$  index; as shown earlier, the effect of varying the  $A_p$  index is small, but exists especially for the Pedersen conductances. We therefore varied  $A_p$  at the same time as the  $f_{10.7}$  index. To do this we averaged the  $A_p$  indices of the last solar cycle at each monthly  $f_{10.7}$  index. Table 2 shows this variation of  $A_p$  versus  $f_{10.7}$  and the numbers used in our modeling.

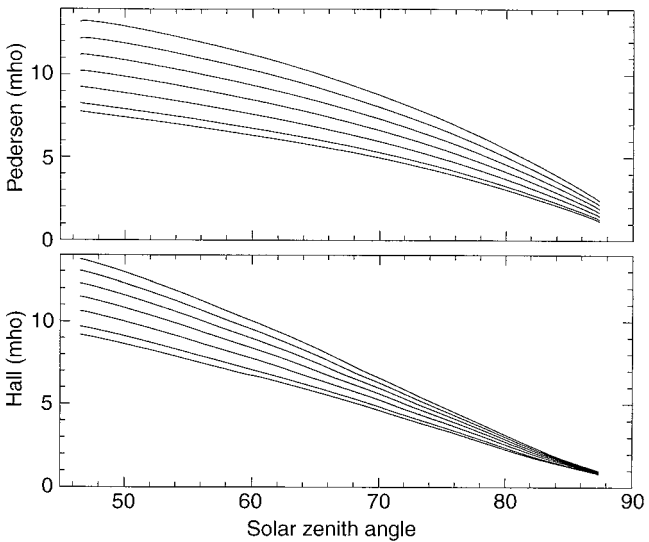
The proper choice of a fitted model has again been studied in Brekke and Hall (1988). With strong physical arguments, they propose a fitted equation for the Hall and Pedersen conductance:  $a \cos \chi + b \cos^{0.5} \chi$ . Indeed, we tried to fit our results with several parametrizations [such as a straight line proposed in Senior (1991) for the Hall conductance,  $\cos \chi$  linear dependence] but found that a polynomial of second order in  $\cos^{0.5} \chi$  gives the best results. Since the coefficients of those polynomials now depend on the solar activity, we let this polynomial have

**Table 2.** Variation of the  $A_p$  index versus  $f_{10.7}$

$\langle f_{10.7} \rangle$	Months of occurrences	$\langle A_p \rangle$	$\langle A_p \text{ used} \rangle$
70	21	13.3	13.5
80	21	14.85	14
90	12	14.75	14.5
100	9	15.3	15
110	5	13.2	15.5
120	7	17.85	16
130	7	18.6	16.5
140	5	13.6	17
150	1	12	17.5
160	2	10.5	18
170	3	20	18.5
180	6	16.2	19
190	5	19.6	19.5
200	9	20.1	20
210	5	22	20.5
220	2	19	21
230	6	20.5	21.5

**Table 3.** The coefficients for our fitted law of conductances

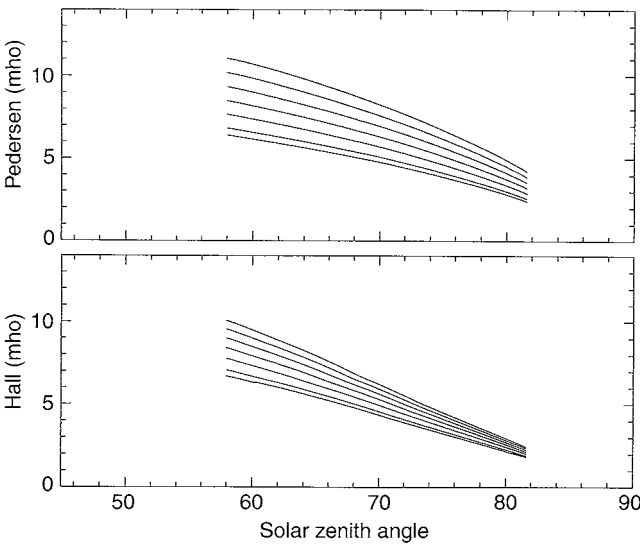
	EISCAT Hall	EISCAT Pedersen	ESR Hall	ESR Pedersen
$a_1$	0.085	0.006	0.109	− 0.004
$a_2$	8.697	2.048	4.713	− 0.017
$b_1$	− 0.022	0.061	− 0.051	0.080
$b_2$	0.222	3.990	4.300	6.331
$c_1$	0.002	− 0.003	0.009	− 0.014
$c_2$	0.227	− 0.560	− 0.858	− 1.205



**Fig. 7.** We show the conductances versus solar zenith angle for seven different solar activities (from bottom to top:  $f_{10.7} = 70, 80, 100, 120, 140, 160, 180$ ) fitted with a second-order polynomial in  $\cos^{0.5} \chi$

an offset. The variation of the coefficients versus  $f_{10.7}$  was considered to be linear (other dependencies proved not to be as precise), so that the generic formula gives:

$$\Sigma_{H,P} = (a_1 f_{10.7} + a_2) \cos \chi + (b_1 f_{10.7} + b_2) \cos^{0.5} \chi + (c_1 f_{10.7} + c_2) \tag{5}$$



**Fig. 8.** Same as Fig. 7 above ESR

The coefficients  $a$ ,  $b$ , and  $c$  are given in Table 3 for EISCAT and ESR, while Figs. 7 and 8 show the conductances for seven different activity levels at Tromsø and Svalbard latitudes ( $f_{10.7} = 70, 80, 100, 120, 140, 160$ , and  $180$ ). The proposed law follows TRANSCAR modeling to less than 5% at any solar angle. The diurnal conductances due solely to photoionization that we predict over ESR are slightly smaller than the conductances over EISCAT for a given solar zenith angle.

Finally, since the conductivity is proportional to the electron density, it is natural to model the altitude below which the electron density is smaller than  $5.10^{10} \text{ m}^{-3}$ , i.e., is no longer detectable by EISCAT (using typical integration times up to 5 mm) by the same kind of laws. This is shown in Fig. 2 as a smoothed line. For solar zenith angles larger than  $60^\circ$ , we found that  $z = 361.8568 \cos \chi - 511.5282 \cos^{0.5} \chi + 278.1$  allows us to compute easily such an altitude.

5 Conclusion

We performed a modeling of the conductances above EISCAT and, in a predictive manner, above ESR, using a coupled fluid/kinetic approach. In order to do so, we first compared successfully our results to the statistical experimental work of Senior (1991). We have shown that EISCAT cannot determine the conductances only due to the solar photoionization for high solar zenith angles with the usual integration times of 1–5 min. Then we studied the influence of various parameters, and finally, we could fit the Hall and Pedersen conductances with a simple second-order polynomial in  $\cos^{0.5} \chi$ . The coefficients of these polynomials depend on the solar activity level  $f_{10.7}$ . This work will be continued in the near future by computing an hour/latitude/activity level conductance model.

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